Under the life-cycle savings hypothesis as developed by Franco Modigliani, the savings ratio (aggregate personal saving divided by disposable income) is explained by per-capita disposable income, the percentage rate of change in per-capita disposable income, and two demographic variables: the percentage of population less than 15 years old and the percentage of the population over 75 years old. The data are averaged over the decade 1960-1970 to remove the business cycle or other short-term fluctuations.

```
data(LifeCycleSavings)
lcs = LifeCycleSavings
dim(lcs) # [1] 50 5
sapply(lcs, function(v) mean(is.na(v)))# sr pop15 pop75 dpi ddpi
# 0 0 0 0 0
?LifeCycleSavings
# sr numeric aggregate personal savings
# pop15 numeric % of population under 15
# pop75 numeric % of population over 75
# dpi numeric real per-capita disposable income
# ddpi numeric % growth rate of dpi
rownames(lcs)[1:5]
#[1] "Australia" "Austria" "Belgium" "Bolivia" "Brazil"
pairs(lcs)
dev.copy(pdf, "BO6pairs.pdf"); dev.off()
```


1: Which predictors look most useful? What transformation might be worth checking? What do you see in terms of outliers (in the X and Y directions)?

```
m0 = lm(sr^*., lcs)summary(m0)
#Coefficients:
# Estimate Std. Error t value Pr(>|t|)
#(Intercept) 28.5660865 7.3545161 3.884 0.000334 ***
#pop15 -0.4611931 0.1446422 -3.189 0.002603 **
#pop75 -1.6914977 1.0835989 -1.561 0.125530
#dpi -0.0003369 0.0009311 -0.362 0.719173
#ddpi 0.4096949 0.1961971 2.088 0.042471 *
#Residual standard error: 3.803 on 45 degrees of freedom
#Multiple R-squared: 0.3385, Adjusted R-squared: 0.2797
```
2: Summarize what you learn from the regression results.

```
library(MASS) # for stepAIC()
m1 = stepAIC(lm(sr^T.^2, lcs))summary(m1)
#Coefficients:
# Estimate Std. Error t value Pr(>|t|)
#(Intercept) 16.5287997 4.3729241 3.780 0.000459 ***
#pop15 -0.2023669 0.0981090 -2.063 0.044943 *
#dpi -0.0027411 0.0011774 -2.328 0.024457 *
#ddpi 0.0462479 0.2439993 0.190 0.850521
#dpi:ddpi 0.0008171 0.0003593 2.274 0.027802 *
#Residual standard error: 3.698 on 45 degrees of freedom
#Multiple R-squared: 0.3745, Adjusted R-squared: 0.3189
```
3: Summarize what you learn from the new regression results.

```
# A residual plotting function
rp = function(mdl, xname=NULL, fname=NULL) {
  res = rstudent(mdl)
  if (is.null(xname)) {
    x = fitted(md1)xname = "Fitted values"
  } else {
    x = \text{mdl}$model[, xname]
  }
  plot(x, res, xlab=xname, ylab="Studentized Residuals",
       main = deparse(substitute(mdl)))
  abline(h=0)
  if (!is.null(fname)) {
    dev.copy(pdf, paste(fname,".pdf",sep=""))
    dev.off()
  }
  invisible(NULL)
}
```
4: Comment on the R code.

rp(m1, fname="BO6RF")

rp(m1, "dpi", "BO6Rdpi")

rp(m1, "ddpi", "BO6Rddpi")

5: Comment on the residual plots

```
summary(influence.measures(m1), digits=2)
#Potentially influential observations of
# lm(formula = sr \sim ., data = lcs) :
# dfb.1_ dfb.pp15 dfb.dpi dfb.ddpi dfb.dp:d
#Luxembourg 0.12 -0.14 0.15 0.07 -0.20
#Netherlands 0.12 -0.15 0.51 0.26 -0.73
#United States 0.01 -0.01 -0.02 0.00 0.00
#Zambia -0.17 0.25 0.06 0.27 -0.13
#Libya 0.09 -0.01 -0.24 -0.51 0.26
#
# dffit cov.r cook.d hat
#Luxembourg 0.25 1.35 0.01 0.19
#Netherlands -0.83 1.49 0.14 0.35
#United States -0.02 1.67 0.00 0.33
#Zambia 0.78 0.39 0.10 0.05
#Libya -0.53 2.98 0.06 0.63
```
6: Comment on the flagged influence measures.

```
library(car) # for influencePlot()
out = influencePlot(m1) # Right click to stop identifying points
dev.copy(pdf, "BO6IP.pdf"); dev.off()
```


7: Comment on the additional, manually flagged influence measures

8: Comment on possible actions to be taken.