# Homework 1: Chicago and Neighbors

### 36-402, Spring 2025

### Due at 6:00 pm on Thursday, 23 January 2025

AGENDA: Remembering how linear regression works; remembering what linear regression can and cannot do; trying out a linear smoother that is not linear regression.

The data set `chicago`, in the package `gamair`, contains data on the relationship between environmental conditions and the death rate in Chicago from 1 January 1987 to 31 December 2000. The seven variables are: the total number of (non-accidental) deaths each day (`death`); the median density over the city of large pollutant particles (`pm10median`); the median density of smaller pollutant particles (`pm25median`); the median concentration of ozone ($O_3$) in the air (`o3median`); the median concentration of sulfur dioxide ($SO_2$) in the air (`so2median`); the time in days (`time`); and the daily mean temperature (`tmpd`).

1. Load the data set and run `summary` on it.

   (a) (1) Is temperature given in degrees Fahrenheit or degrees Celsius?

   (b) (1) The pollution variables are negative at least half the time. What might this mean?

2. *Death over time*

   (a) (5) Plot the number of deaths versus the time. Describe any patterns you see. *Hint:* The plot becomes easier to interpret if you make the horizontal axis the calendar date. What does the following code fragment do?

   ```
   day.zero <- as.Date("1993-12-31")
   chicago$date <- day.zero + chicago$time
   ```

   (b) (2) Linearly regress the number of deaths on time. Add the regression line to the previous plot. Report the slope coefficient (to reasonable precision). Is it significantly different from zero?

   (c) (2) Carefully explain the interpretation of the regression slope.

   (d) (3) Plot the residuals against the time. Describe any patterns you see.

   (e) (2) Is there any reason to doubt the validity of the significance test here?

3. *Neighbors in time* Install the package `FNN`, and use the `knn.reg` function when asked to do *k*-nearest neighbors. *Hint:* Figure 1.5 in the textbook, and the accompanying code. In particular, the `test` argument to `knn.reg` should (in this case) be a one-column matrix.

   (a) (5) Do a *k*-nearest-neighbor regression of death on time, using $k = 3$ nearest neighbors. Generate a predicted value for each day in the data set. Use these predicted values to add the estimated regression function to the plot you made in Q2b. Describe the shape of the estimated function.

   (b) (5) Carefully explain, in your own words, how the predicted values in Q3a are derived from the original data.

   (c) (3) Repeat Q3a for $k = 30$. Describe how (if at all) the new estimate of the curve differs from the old.

4. *Death likes it cold?*

   (a) (3) Plot the number of deaths against temperature. Describe any patterns you see.

   (b) (4) Linearly regress the number of deaths on temperature. Add the regression line to the previous plot; report the slope coefficient (to reasonable precision).

   (c) (2) Carefully explain the interpretation of the slope coefficient.

   (d) (5) Re-create the plot from Q2b, and add a curve showing the predicted values from the new linear regression on temperature as a function of time. Describe the pattern that you see. Which linear regression does a better job of *explaining* the data, the one on time or the one on temperature? Why?

   (e) (4) Plot the residuals of the regression of deaths on temperature. Describe any patterns you see.

5. *Death likes it hot also?* Refer to Q3 for hints on using `knn.reg`.

   (a) (5) Do a 30-nearest neighbor regression of the number of deaths on temperature. Generate predictions at values of temperature that span the observed range in the data set. Use these predictions to add the estimated regression function to the plot you made in Q4b. *Hint:* If your plot looks weird, look carefully at Figure 1.5 in the textbook again.

   (b) (5) Describe the shape of the estimated regression function, and contrast it with the linear regression. What are the *qualitative* differences between the two estimates here?

   (c) (5) Re-create the plot from Q3a, and add the predicted values for each day from the 30-nearest-neighbor regression on temperature. Describe the shape of the new curve over time. Which model does a better job of explaining the data, the nearest neighbor regression on time from Q3a or the nearest neighbor regression on temperature? Why?

6. *Hypotheticals* Many climate models predict that the Chicago area might, by the end of the 21st century, be 4.5 degrees Celsius warmer than the time-period in which this data was collected.

   (a) (1) Add a new column to the `chicago` data frame, which takes each day's observed temperature, and makes it 4.5 degrees Celsius hotter. Give the code you used, and a brief explanation of why that code does the right thing. *Hint:* The temperatures are in Farenheit. A *change* of 4.5 degrees Celsius, expressed in Farenheit, is not the same as adding the Farenheit temperature that corresponds to 4.5 degrees Celsius. (Why not?) Consequently, Googling "4.5 degrees Celsius in Farenheit" will give you very misleading answers.

   (b) (5) Use the linear model you estimated in Q 4b to estimate the change in the number of people predicted to die on each day in the data, and report the average change. *Hint 1:* Do *not* re-estimate the model with the new column as the predictor variable. *Hint 2:* You could use `predict` to get predictions at the old, observed temperature, and the new, hypothetical temperature, and take the difference. (See the handout on "`predict` and Friends" on the class homepage under Lecture 2.) *Hint 3:* There is a faster way to do this for the linear model.

   (c) (5) Use the 30-nearest-neighbor regression you estimated in Q5a to estimate the change in the number of people predicted to die on each day in the data, and report the average change. *Hint 1:* Do *not* re-estimate the model with the new column as the predictor variable. *Hint 2:* Use the `test` argument of `knn.reg` to get predictions at values which might or might not be in the data set.

7. (3) Exercise 1.7 from the textbook.

8. (4) Exercise 1.8.

9. (4) Exercise 1.9.

10. (5) Exercise 1.10.

11. (1) How much time, roughly, did you spend on this homework?

The last few problems need you to write out math. Please see the handout "Using R Markdown for Class Reports" (`http://www.stat.cmu.edu/~cshalizi/rmarkdown/`, link on the syllabus) for assistance in doing so. If you just can't make it work, please write out the math by hand, scan it, and include the scans in your submission. You will not lose points for doing so *this* time; as the semester goes on, the penalty for hand-written math will increase. (You will lose points this time if your hand-written math is excessively hard to read.) Do not use Word for math.

PRESENTATION RUBRIC (10): The text is laid out cleanly, with clear divisions between problems and sub-problems. The writing itself is well-organized, free of

grammatical and other mechanical errors, and easy to follow. Plots are carefully labeled, with informative and legible titles, axis labels, and (if called for) sub-titles and legends; they are placed near the text of the corresponding problem. All plots and tables are generated by code included in the R Markdown file. All quantitative and mathematical claims are supported by appropriate derivations, included in the text, or calculations in code. Numerical results are reported to appropriate precision. All parts of all problems are answered with actual coherent sentences, and raw computer code or output are only shown when explicitly asked for. Text from the homework assignment, including this rubric, is included only when relevant, not blindly copied.