

Multi-level:

$$\begin{aligned}
\text{Classical}_i &= \alpha_{0j[i]} + \alpha_{guitar,j[i]} \cdot 1_{\{\text{Instrument}_i=\text{guitar}\}} + \alpha_{piano,j[i]} \cdot 1_{\{\text{Instrument}_i=\text{piano}\}} + \alpha_{string,j[i]} \cdot 1_{\{\text{Instrument}_i=\text{string}\}} + \\
&\quad \alpha_{contrary,j[i]} \cdot 1_{\{\text{Voice}_i=\text{contrary}\}} + \alpha_{par3rd,j[i]} \cdot 1_{\{\text{Voice}_i=\text{par3rd}\}} + \alpha_{par5th,j[i]} \cdot 1_{\{\text{Voice}_i=\text{par5th}\}} + \\
&\quad \alpha_{I-IV-V,j[i]} \cdot 1_{\{\text{Harmony}_i=\text{I-IV-V}\}} + \alpha_{I-V-IV,j[i]} \cdot 1_{\{\text{Harmony}_i=\text{I-V-IV}\}} + \\
&\quad \alpha_{I-V-VI,j[i]} \cdot 1_{\{\text{Harmony}_i=\text{I-V-VI}\}} + \alpha_{IV-I-V,j[i]} \cdot 1_{\{\text{Harmony}_i=\text{IV-I-V}\}} + \epsilon_i, \quad \epsilon_i \stackrel{iid}{\sim} N(0, \sigma^2) \\
\alpha_{0j} &= \beta_0 + \eta_{0j}, \quad \eta_{0j} \stackrel{iid}{\sim} N(0, \tau_0^2) \\
\alpha_{guitar,j} &= \beta_{guitar} + \eta_{guitar,j}, \quad \eta_{guitar,j} \stackrel{iid}{\sim} N(0, \tau_{guitar}^2) \\
\alpha_{piano,j} &= \beta_{piano} + \eta_{piano,j}, \quad \eta_{piano,j} \stackrel{iid}{\sim} N(0, \tau_{piano}^2) \\
\alpha_{string,j} &= \beta_{string} + \eta_{string,j}, \quad \eta_{string,j} \stackrel{iid}{\sim} N(0, \tau_{string}^2) \\
\alpha_{contrary,j} &= \beta_{contrary} + \eta_{contrary,j}, \quad \eta_{contrary,j} \stackrel{iid}{\sim} N(0, \tau_{contrary}^2) \\
\alpha_{par3rd,j} &= \beta_{par3rd} + \eta_{par3rd,j}, \quad \eta_{par3rd,j} \stackrel{iid}{\sim} N(0, \tau_{par3rd}^2) \\
\alpha_{par5th,j} &= \beta_{par5th} + \eta_{par5th,j}, \quad \eta_{par5th,j} \stackrel{iid}{\sim} N(0, \tau_{par5th}^2) \\
\alpha_{I-IV-V,j} &= \beta_{I-IV-V} + \eta_{I-IV-V,j}, \quad \eta_{I-IV-V,j} \stackrel{iid}{\sim} N(0, \tau_{I-IV-V}^2) \\
\alpha_{I-V-IV,j} &= \beta_{I-V-IV} + \eta_{I-V-IV,j}, \quad \eta_{I-V-IV,j} \stackrel{iid}{\sim} N(0, \tau_{I-V-IV}^2) \\
\alpha_{I-V-VI,j} &= \beta_{I-V-VI} + \eta_{I-V-VI,j}, \quad \eta_{I-V-VI,j} \stackrel{iid}{\sim} N(0, \tau_{I-V-VI}^2) \\
\alpha_{IV-I-V,j} &= \beta_{IV-I-V} + \eta_{IV-I-V,j}, \quad \eta_{IV-I-V,j} \stackrel{iid}{\sim} N(0, \tau_{IV-I-V}^2)
\end{aligned}$$

Hierarchical:

It's actually somewhat difficult to write the Hierarchical model efficiently. One way would be to define

$$\begin{aligned}
m_i &= \alpha_{0j[i]} + \alpha_{guitar,j[i]} \cdot 1_{\{\text{Instrument}_i=\text{guitar}\}} + \alpha_{piano,j[i]} \cdot 1_{\{\text{Instrument}_i=\text{piano}\}} + \alpha_{string,j[i]} \cdot 1_{\{\text{Instrument}_i=\text{string}\}} + \\
&\quad \alpha_{contrary,j[i]} \cdot 1_{\{\text{Voice}_i=\text{contrary}\}} + \alpha_{par3rd,j[i]} \cdot 1_{\{\text{Voice}_i=\text{par3rd}\}} + \alpha_{par5th,j[i]} \cdot 1_{\{\text{Voice}_i=\text{par5th}\}} + \\
&\quad \alpha_{I-IV-V,j[i]} \cdot 1_{\{\text{Harmony}_i=\text{I-IV-V}\}} + \alpha_{I-V-IV,j[i]} \cdot 1_{\{\text{Harmony}_i=\text{I-V-IV}\}} + \\
&\quad \alpha_{I-V-VI,j[i]} \cdot 1_{\{\text{Harmony}_i=\text{I-V-VI}\}} + \alpha_{IV-I-V,j[i]} \cdot 1_{\{\text{Harmony}_i=\text{IV-I-V}\}}
\end{aligned}$$

and then write, ignoring the correlations again,

$$\begin{aligned}
\text{Classical}_i &\sim N(m_i, \sigma^2) \\
\alpha_{0j} &\sim \beta_0 + \eta_{0j}, \quad \eta_{0j} \stackrel{iid}{\sim} N(0, \tau_0^2) \\
\alpha_{guitar,j} &\sim N(\beta_{guitar}, \tau_{guitar}^2) \\
\alpha_{piano,j} &\sim N(\beta_{piano}, \tau_{piano}^2)
\end{aligned}$$

$$\begin{aligned}
\alpha_{string,j} &\sim N(\beta_{string}, \tau_{string}^2) \\
\alpha_{contrary,j} &\sim N(\beta_{contrary}, \tau_{contrary}^2) \\
\alpha_{par3rd,j} &\sim N(\beta_{par3rd}, \tau_{par3rd}^2) \\
\alpha_{par5th,j} &\sim N(\beta_{par5th}, \tau_{par5th}^2) \\
\alpha_{I-IV-V,j} &\sim N(\beta_{I-IV-V}, \tau_{I-IV-V}^2) \\
\alpha_{I-V-IV,j} &\sim N(\beta_{I-V-IV}, \tau_{I-V-IV}^2) \\
\alpha_{I-V-VI,j} &\sim N(\beta_{I-V-VI}, \tau_{I-V-VI}^2) \\
\alpha_{IV-I-V,j} &\sim N(\beta_{IV-I-V}, \tau_{IV-I-V}^2)
\end{aligned}$$

A fully correct specification would express the random vector of  $\alpha$ 's as a multivariate normal, like this for the model with random effects (`Instrument + Voice + Harmony || Subject`), for example:

$$\left[ \begin{array}{l} \alpha_0 \\ \alpha_{guitar,j} \\ \alpha_{piano,j} \\ \alpha_{string,j} \\ \alpha_{contrary,j} \\ \alpha_{par3rd,j} \\ \alpha_{par5th,j} \\ \alpha_{I-IV-V,j} \\ \alpha_{I-V-IV,j} \\ \alpha_{I-V-VI,j} \\ \alpha_{IV-I-V,j} \end{array} \right] \stackrel{iid}{\sim} N \left( \begin{array}{l} \beta_0 \\ \beta_{guitar} \\ \beta_{piano} \\ \beta_{string} \\ \beta_{contrary} \\ \beta_{par3rd} \\ \beta_{par5th} \\ \beta_{I-IV-V} \\ \beta_{I-V-IV} \\ \beta_{I-V-VI} \\ \beta_{IV-I-V} \end{array} \right), \left[ \begin{array}{llllllllll} \tau_{0j} & & & & & & & & & \\ 0 & \tau_{guitar}^2 & & & & & & & & \\ 0 & \rho_{gp} & \tau_{piano}^2 & & & & & & & \\ 0 & \rho_{gs} & \rho_{ps} & \tau_{string}^2 & & & & & & \\ 0 & 0 & 0 & 0 & \tau_{contrary}^2 & & & & & \\ 0 & 0 & 0 & 0 & \rho_{c3} & \tau_{par3rd}^2 & & & & \\ 0 & 0 & 0 & 0 & \rho_{c5} & \rho_{35} & \tau_{par5th}^2 & & & \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & \tau_{I-IV-V}^2 & & \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & \rho_{145,154} & \tau_{I-V-IV}^2 & \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & \rho_{145,156} & \rho_{154,156} & \tau_{I-V-VI}^2 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & \rho_{145,415} & \rho_{154,415} & \rho_{156,415} & \tau_{IV-I-V}^2 \end{array} \right] \quad (\text{symmetric})$$

and the model with random effects (`Instrument + Voice + Harmony | Subject`) would look the same, except the 0's in the variance-covariance matrix above would be replaced with additional correlations.