36-303: Sampling, Surveys and Society

Variance Calculations for Weights Brian W. Junker 132E Baker Hall brian@stat.cmu.edu

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Handouts These Lecture Notes Also an R handout! Post-Stratification Challenges Handout Handouts on the Census [read first!] Farley – Statistical, Political and Constitutional

- Farley Statistical, Political and Constitutional Issues in the Census Undercount
 USAToday: Q&A: 2010 Census
- Fort Worth Star Telegram: Census Undercount Could Cost Texas Money, Political Clout

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Calculating the Variances for TS Method... If we assume that each pair (w_iy_i, w_i) is independent of every other pair (not quite true but close!) then $Var(\sum_{i=1}^{n} w_i) = \sum_{i=1}^{n} Var(w_i) = nVar(w) \approx n \cdot \frac{1}{n-1} \sum_{i=1}^{n} (w_i - \overline{w})^2 = n \cdot s_w^2$ where $\overline{w} = \frac{1}{n} \sum_i w_i$. Similarly, $Var(\sum_{i=1}^{n} y_i w_i) \approx n \cdot \frac{1}{n-1} \sum_{i=1}^{n} (w_i y_i - \overline{wy})^2 = n \cdot s_{wy}^2$ where $\overline{wy} = \frac{1}{n} \sum_i w_i y_i$, and $Cov(\sum_{i=1}^{n} y_i w_i, \sum_{i=1}^{n} w_i) \approx n \cdot \frac{1}{n-1} \sum_{i=1}^{n} (w_i y_i - \overline{wy})(w_i - \overline{w}) = n \cdot s_{wy,w}$

Example: HSS Advising Survey									
DICL	Adv'ing	Samp	D	Pop	D	TT 7 • 1 /			
Post-Strat.	OK	Total	Prop	Total	Prop	Weights			
Economics	28	40	0.132	126	0.128	0.97			
English	23	39	0.128	115	0.117	0.91			
History	10	21	0.069	48	0.049	0.70			
ModLang	3	8	0.026	16	0.016	0.62			
Philosophy	1	4	0.013	7	0.007	0.54			
Psychology	11	37	0.122	104	0.105	0.87			
SDS	22	54	0.178	161	0.163	0.92			
Statistics	3	6	0.020	8	0.008	0.41			
Interdisc/IS	46	76	0.250	233	0.236	0.95			
Undeclared	13	19	0.062	168	0.170	2.73			
Total	160	304		986					
weight = (Population Proportion) / (Sample Proportion)									
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Example: HSS Advising Data (Again)									
Doot Strat	Adv'ing	Samp	Duon	Pop	Duan	Weighte			
Post-Strat.	UK	Iotal	Prop	Iotal	Prop	weights			
Economics	28	40	0.132	126	0.128	0.97			
English	23	39	0.128	115	0.117	0.91			
History	10	21	0.069	48	0.049	0.70			
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